



# BK BIRLA CENTRE FOR EDUCATION

SARALA BIRLA GROUP OF SCHOOLS  
SENIOR SECONDARY/CO-ED DAY CUM BOYS' RESIDENTIAL SCHOOL

MID-TERM EXAMINATION 2023-24

MATHEMATICS (041)



Class : XI SC  
Date : 11/09/23  
Admission No:

## MARKING SCHEME

Duration: 3 Hrs  
Max. Marks: 80  
Roll No. :

- |   |   |
|---|---|
| 1. C) $(A \cup B) - (A \cap B)$   | 1 |
| 2. B) $B \subseteq A$   | 1 |
| 3. C) $\emptyset$   | 1 |
| 4. C) $2f(x)$   | 1 |
| 5. C) $R - \left\{-\frac{1}{2}, 1\right\}$  | 1 |
| 6. C) 3   | 1 |
| 7. D) none of these   | 1 |
| 8. C) $\tan 3x$   | 1 |
| 9. C) $\frac{\sqrt{3}}{2}$  | 1 |
| 10. B) 0  | 1 |
| 11. A) $\frac{\pi}{4}$  | 1 |
| 12. B) $2i$   | 1 |
| 13. B) $-5 < x < 5$   | 1 |
| 14. D) 69760  | 1 |
| 15. B) 1956   | 1 |
| 16. C) 7200   | 1 |
| 17. D) 7920   | 1 |
| 18. B) -1365  | 1 |
| 19. D   | 1 |
| 20. A   | 1 |
| 21. $A - B = \{3, 6, 15, 18, 21\}$  | 2 |
| 22. $X=3, Y=-1,$<br>OR $x=\pm 5$  | 2 |
| 23. $\sin \frac{\pi}{12} = \sin \left(\frac{\pi}{4} - \frac{\pi}{6}\right) = \frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}} \times \frac{1}{2} = \frac{\sqrt{3}-1}{2\sqrt{2}}$<br>OR<br>$\tan \frac{13\pi}{12} = \tan \left(\pi + \frac{\pi}{12}\right) = \tan \frac{\pi}{12} = \frac{\sqrt{3}-1}{\sqrt{3}+1}$ | 2 |
| 24. $4 \times 4 \times 4 \times 4 \times 4 = 4^5$   | 2 |
| 25. $n=9$ , no. of terms = $n+1 = 9+1=10$ .   | 2 |
| 26. $A' \cap B' = (A \cup B)' = n(U) - n(A \cup B) = 700 - 400 = 300$ .   | 3 |
| 27. $ x - 3  > 0, 0 \leq  x - 3  < \infty, f(x) = [0, \infty)$ .  |   |
| OR  |   |
| $(1, 4), (1, 5), (2, 4), (2, 5), (3, 4), (3, 5), (4, 5)$ .  | 3 |
| 28. $\frac{2 \sin 4x \cos x}{2 \cos 4x \cos x} = \frac{\sin 4x}{\cos 4x} = \tan 4x$ ,   |   |
| OR  |   |

$$\cot(570^\circ) = \cot(540^\circ + 30^\circ) = \cot 30^\circ = \sqrt{3}$$

3

29.  $i^9 + i^{19} = i + i^3 = i - i = 0.$

**OR**

$$(x+iy)(2-3i) = 4+i$$

$$(2x+3y) - (3x-2y)i = 4+i$$

On comparing  $x=5/13, y=14/13.$

3

30.  ${}^9P_5 + 5 \cdot {}^9P_4 = {}^{10}P_r = \frac{9!}{4!} + 5 \frac{9!}{5!} = \frac{10!}{(10-r)!} = 5! = (10-r)! = r=5.$

3

31.  $T_{17} = {}^{50}C_{16} 2^{34} x a^{16},$

$$T_{18} = {}^{50}C_{17} 2^{33} x a^{17},$$

$$a = \frac{50!}{34!16!} x \frac{33!x17!}{50!} \times 2$$

$$\frac{34}{34} = 1.$$

3

32. It is given that 65 students offered Physics  $(40-x)+x+(20-x)+8 = 65, x=3$

i) Offered Math =  $15+(10-x) + x+40-x = 62$

ii) Offered statistics =  $12+(10-x) + x+(20-x) = 39$

5

iii) Offered any of three subjects = 99, there for did not offered any of three subject =  $100-1=99.$

33.  $(\cos x + \cos y)^2 + (\sin x - \sin y)^2 = 1+1+2\cos x \cos y - 2\sin x \sin y = 2+2[\cos(x+y)] = 2[1 + \cos(x+y)] = 2\cos^2(x+y/2).$

5

**OR**

LHS:  $\cot 4x(\sin 5x + \sin 3x) = \cot 4x(2\sin 4x \cos x) = 2\cos 4x \cos x$

RHS:  $\cot x(\sin 5x - \sin 3x) = \cot x(2\sin x \cos 4x) = 2\cos 4x \cos x.$

34.  $\frac{5x-2}{3} - \frac{7x-3}{5} > \frac{x}{4} = \frac{25x-10-21x+9}{15} > \frac{x}{4} = 16x-15x > 4 = x > 4, x \in (4, \infty)$

**OR**

$5x-3 < 3x+1 = 2x < 4, x < 2$

i)  $x \in (-\infty, 2)$  ii)  $x = 1, 0, -1, -2, -3, -4, \dots$  iii)  $x = 1$

5

35. i)  ${}^{52}C_4 = 270725$  , ii)  $4 \cdot {}^{13}C_4 = 2860$  , iii)  $13^4$

5

36. i) 8 ways, ii) 1000 ways, ii) 720 ways

1+1+2

37. i)  $a=6, b=0$  , ii)  $x=-6, y=8$  , iii)  $A \times B \neq B \times A$

1+1+2

38. i)  $10+0+3+5 = 18$  , ii)  $0+3=3$ , iii) 3

1+1+2

